



**ST HILDA'S**  
ANGELICAN SCHOOL FOR GIRLS INC.

<b>Total Time:</b>	25 minutes
<b>Marks:</b>	22 marks
<b>Total Marks:</b>	$\frac{\quad}{40}$

**Methods 3&4**  
**Review Response Test 1**  
(Wed Mar 31<sup>st</sup>)

**Resource Free**

ClassPad calculators are NOT permitted.  
Formulae sheet is permitted.

**Name:** \_\_\_\_\_

**1. [1, 2 & 2 = 5 marks]**

Find the following indefinite integrals.

**(a)**  $\int 4\sqrt{x} \, dx$

**(b)**  $\int (3x-2)^3 \, dx$

**(c)**  $\int (x^2 + 2)^2 \, dx$

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**2. [4 marks]**

Find the area bounded between the graph of  $y = 3x(x-4)$  and the  $x$ -axis.

**3. [3 marks]**

Find the equation of the tangent to the curve  $y = \frac{2x-1}{x-1}$  at the point (2, 3) giving your answer in the form  $y = mx + c$ .

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**4. [4 marks]**

Find the  $x$ -coordinates of the points on the graph of  $y = x^2(2x+3)$  where the gradient is 12.

**5. [6 marks]**

Use calculus techniques to determine the coordinates, and their nature, of any stationary points on the curve with equation  $y = 2x + \frac{18}{x}$ .



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**Total Time:** 20 minutes

**Marks:** 18 marks

**Methods 3&4**  
**Review Response Test 1**  
(Wed Mar 31<sup>st</sup>)

**Resource Assumed**

ClassPad calculators ARE permitted.  
Formulae sheets are permitted.

**Name:** \_\_\_\_\_

**6. [4 marks]**

Given that  $f(x) = ax^3 + bx^2 + 2x + 1$ ,  $f'(1) = 9$  and  $f''\left(\frac{1}{3}\right) = 4$ , find the value of the constants  $a$  and  $b$ .

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**7. [3 marks]**

Showing the use of definite integrals (without absolute value), find the area enclosed between the graphs of  $y_1 = 3x + 6$  and  $y_2 = x(x + 2)(x - 2)$

8. [2, 2 & 1 = 5 marks]

(a) Find the coordinates of the points where the curve  $y = \frac{3x^2}{2x+1}$  cuts the line  $y = 2x - 1$ .

(b) Find the gradient of curve  $y = \frac{3x^2}{2x+1}$  at each point where it cuts the line  $y = 2x - 1$ .

(c) Find the equation of the tangent to the curve  $y = \frac{3x^2}{2x+1}$  at the point with x-coordinate of 2.

**9. [6 marks]**

The owner of a garden centre wishes to fence a rectangular area of  $360 \text{ m}^2$ . She wishes to fence three sides with fencing that costs  $\$5/\text{m}$  and the fourth side with fencing costing  $\$11/\text{m}$ .

Show the use of calculus to find the dimensions of the rectangular area that will minimise her fencing costs.